22103

21819 3 Hours / 70 Marks

Seat No.									
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Instructions : (1) All Questions are *compulsory*.

- (2) Illustrate your answers with neat sketches wherever necessary.
- (3) Figures to the right indicate full marks.
- (4) Mobile Phone, Pager and any other Electronic Communication devices are not permissible in Examination Hall.

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1. Attempt any FIVE of the following :

(a) Prove that
$$\frac{1}{\log_3 6} + \frac{1}{\log_8 6} + \frac{1}{\log_9 6} = 3$$
.

(b) Find x, if
$$\begin{vmatrix} 4 & 3 & 9 \\ 3 & -2 & 7 \\ 11 & 4 & x \end{vmatrix} = 0.$$

- (c) Without using calculator, find the value of $\cos(105^\circ)$.
- (d) The area of a rectangular garden is 3000 m². Its sides are in the ratio 6 : 5.
 Find the perimeter of the garden.
- (e) Find the area of ring between two concentric circles whose circumferences are 75 cm and 55 cm.
- (f) Find the range and coefficient of range 40, 52, 47, 28, 45, 36, 47, 50.
- (g) The two sets of observations are given below :

 Set I
 Set II

 $\overline{x} = 82.5$ $\overline{x} = 48.75$
 $\sigma = 7.3$ $\sigma = 8.35$

Which of two sets is more consistent?

2. Attempt any THREE of the following :

(a) Solve the equations by Cramer's rule :

$$x + y + z = 3$$
, $x - y + z = 1$, $x + y - 2z = 0$

(b) If
$$A = \begin{bmatrix} 2 & 4 & 4 \\ 4 & 2 & 4 \\ 4 & 4 & 2 \end{bmatrix}$$
, find $A^2 - 8A$.

(c) Resolve into partial fractions

$$\frac{3x+2}{(x+1)(x^2-1)}$$

(d) A metal strip having sides 17 × 7× 5 cm is melted down and minted into coins each of diameter 1.4 cm and thickness 0.08 cm. Assuming no wastage, how many coins can be minted ?

3. Attempt any THREE of the following :

(a) Prove that

 $\tan 70^\circ - \tan 50^\circ - \tan 20^\circ = \tan 70^\circ \tan 50^\circ \tan 20^\circ$.

(b) Prove that
$$\frac{1+\sin\theta-\cos\theta}{1+\sin\theta+\cos\theta} = \tan\left(\frac{\theta}{2}\right)$$
.

(c) Prove that
$$\frac{\cos 2A + 2\cos 4A + \cos 6A}{\cos A + 2\cos 3A + \cos 5A} = \cos A - \sin A \tan 3A$$

- (d) Prove that
 - $\sin 20^{\circ} \sin 40^{\circ} \sin 60^{\circ} \sin 80^{\circ} = \frac{3}{16}$

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4. Attempt any THREE of the following :

(a) Find the adjoint of matrix

$$\mathbf{A} = \begin{bmatrix} 2 & 5 & 3 \\ 3 & 1 & 2 \\ 1 & 2 & 1 \end{bmatrix}$$

(b) Resolve into partial fractions

$$\frac{x^4}{x^3+1}$$

(c) Prove that $\tan^{-1}(1) + \tan^{-1}(2) + \tan^{-1}(3) = \pi$.

(d) Prove that

$$\sin^{-1}\left(\frac{3}{5}\right) - \sin^{-1}\left(\frac{8}{17}\right) = \cos^{-1}\left(\frac{84}{85}\right)$$

(e) Without using calculator, prove that $\sin 420^{\circ} \cos 390^{\circ} + \cos (-300^{\circ}) \sin (-330^{\circ}) = 1$

5. Attempt any TWO of the following :

- (a) Attempt the following :
 - (i) Find the acute angle between the lines y = 5x + 6 and y = x.
 - (ii) Find the equation of the line passing through the point (4,5) and perpendicular to the line 7x 5y = 420.
- (b) Attempt the following :
 - (i) Find the length of perpendicular from the point (2,3) on the line 4x 6y 3 = 0.
 - (ii) Find the equation of the line passing through (1,7) and having slope 2 units.

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- (c) Attempt the following :
 - (i) A square grassy plot is of side 100 metres. It has a gravel path 10 meters wide all round it on the inside. Find the area of the path.

(ii) The volume of a sphere is
$$\frac{88}{21}$$
 cubic meters. Find its surface area.

6. Attempt any TWO of the following :

(a) (i) Find the mean deviation from mean of the following distribution :

	C.I.	0 – 10	10-20	20-30	30-40	40 - 50
F	f_i	5	8	15	16	6

(ii) Find range & coefficient of range for the following data :

C.I.	10 - 19	20 - 29	30 - 39	40 - 49	50 - 59
f	15	25	13	17	10

(b) Calculate standard deviation and coefficient of variance of the following table :

Marks below	5	10	15	20	25
No. of Students	6	16	28	38	46

(c) Solve the following equations by using matrix inversion method :

x + y + z = 6, 3x - y + 3z = 10, 5x + 5y - 4z = 3

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